

Modeling the effects of electrical conductivity of the head on the induced electric field in the brain during magnetic stimulation

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Abstract

Objective: The objective of this document is to quantify the effect of changing conductivity within the brain in transcranial magnetic stimulation.

Methods: Extreme examples of white and grey matter distributions as well as cerebral spinal fluid are analyzed with numerical boundary element methods to show that the induced E fields for these various distributions vary little from the homogeneous case.

Results: Models representative of the brain that demarcate regions of white matter and grey matter add an unnecessary level of complexity to the design and analysis of magnetic stimulators. The induced E field varies little between a precise model with exact placement of white and grey matter from that of its homogeneous counterpart. The E field will increase in white matter, and decrease in grey, but the variation is small. The contour integral of the E field around a closed path is dictated by the flux change through that contour.

Discussion: The maximum value of the variation of the electric field between a fully homogeneous medium, and one filled with different conductivity media is 1/2 the conductivity ratio of the media involved. Neuronal stimulation is more likely at the interface between dissimilar mediums, the greatest being between white matter and cerebral spinal fluid. The interface location where no normal electric field exists will witness a localized electric field 51% greater than the homogeneous E field on the white matter side of that interface. White–grey matter interfaces will have a maximum localized increase in the E field 22.9% greater than the homogeneous case.

Conclusions: Variations in neural intracellular potential during a magnetic stimulation pulse will be small among patients. The most efficient modeling will follow by assuming the medium homogeneous, and noting that perturbations from this result will exist.

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1. Background

Magnetic stimulation of the human brain is now common practice both as a research and a diagnostic tool, and is being increasingly employed in the treatment of depression (Epstein and Davey, 2002). In TMS, a time varying magnetic field held near the scalp induces electrical currents in brain. An important question for researchers in this arena is determining exactly where in the brain TMS induces electrical activity, and whether this shifts as a function of differences in conductivity and organization of grey matter,

white matter and CSF (Bohning et al., 1997, 2001; Analylist et al., submitted for publication; Wassermann et al., 1996). A number of effective homogeneous models of the TMS magnetic field have been proposed (Roth and Basser, 1990; Ueno et al., 1988, 1990). Liu and Ueno (1998) proposed that when current flow from a lower conductivity region to a higher one, the interface acts as a virtual cathode. An analogy is then drawn to infer the similarities between conventional electric stimulation and magnetic.

This manuscript would support that inference and underscore the fact that at the point that positive ions are driven into a nerve cell, its intracellular potential will rise, and if the rise is sufficient, an action potential results. The electric field is larger on the lower conductivity region.

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The nerve cell cannot distinguish whether the rise occurred because of a rapidly changing magnetic field or an imposed electric field. The inner skull boundary condition insures that the normal component of current density is essentially zero on that boundary.

2. Methods

Several models are tested to determine how the inclusion of volume conductivity differences affects the induced electric field. The analyses are performed using numerical boundary element methods (Zheng, 1997). In this technique equivalent surface sources are sought to satisfy Ampere’s and Faraday’s law in the medium and the boundary conditions on the surface. Both surface current and surface charge are required on every interface. The induced E field is proportional to frequency; the frequency is held fixed at 5740 Hz in all calculations as are the amp-turns. The brain is represented as a 7.5 cm radius sphere. Due to symmetry only 1/4 of both the C core stimulator and the target is modeled.

After each computation, the induced E field was determined throughout the brain twice, the second time with a homogeneous conductivity throughout. The numerical solver has the ability to compute and display the E field at a number of preset densities. Although the density was held fixed throughout this study, the number of comparison points changes slightly due to the program’s need to vary the location of the computed E field as discrete region volumes change.

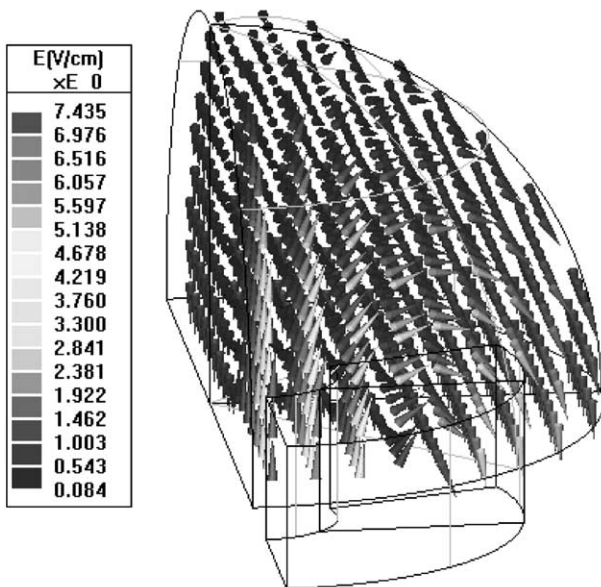


Fig. 1. Homogeneous model of the brain with conductivity 0.75 S/m throughout.

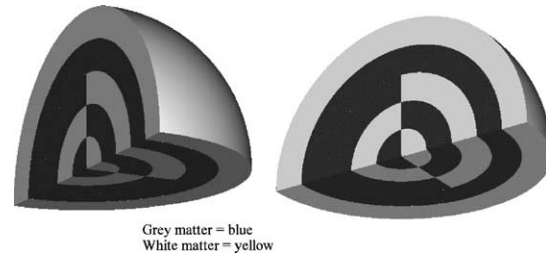


Fig. 2. Concentric sphere distribution of grey and white matter.

3. Results

3.1. Homogeneous model

Consider first the homogeneous model shown in Fig. 1. The brain is depicted as a homogeneous sphere with radius 7.5 cm. The outer surface corresponds to the skull. 1/4 of the problem is worked due to symmetry. The arrows depict how the E field curls around the flux face of the magnet. When the conductivity is dropped in half to 0.37 S/m, the resulting E field differs from Fig. 1 by a maximum of 0.17%. This was computed by breaking the 1/4 brain region into 778 subvolumes and computing the E field at the center of those volumes.

3.2. Inhomogeneous model 1—concentric spheres

According to Polk and Postow (1996), the conductivity of white and grey matter is 0.48 and 0.7 S/m, respectively. Consider positioning the grey and white matter as a number of concentric spherical bands as shown in Fig. 2. The band pattern was intentionally altered so that the two 1/8 sections would themselves exhibit a contrast.

The surface E field obtained from this model is shown in Fig. 3. Shown in Fig. 4 is a plot of the E field predicted at 3528 points within the volume of this model. The mean absolute value of the difference between these two models is

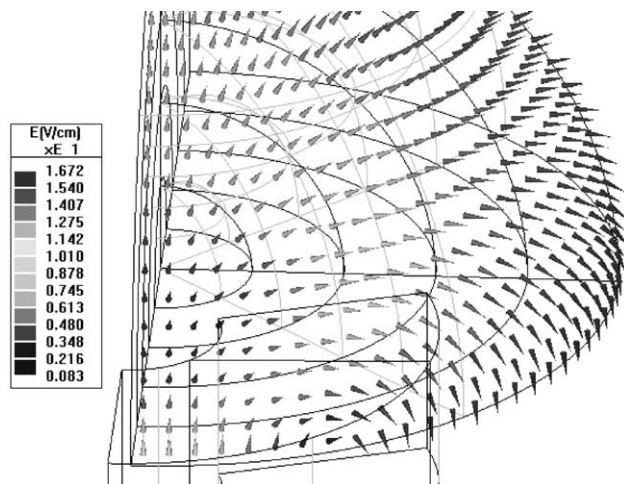


Fig. 3. Surface E field plot for the spherical distribution of white and grey matter.

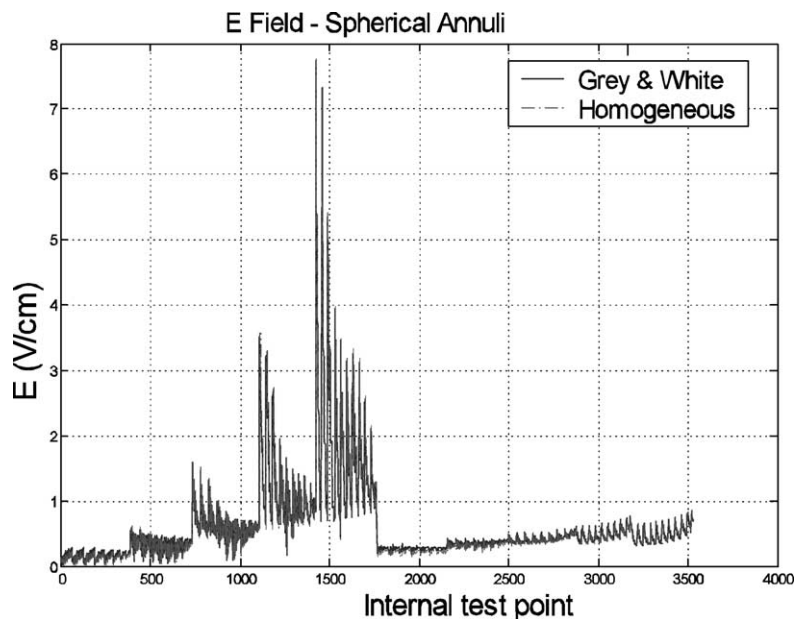


Fig. 4. Comparison of homogeneous and inhomogeneous E fields for a spherical annulus model.

6.8%. Fig. 1 does not account for the differences in grey and white matter, while Fig. 2 does make such a distinction.

Performing a comparison within a volume is challenging, especially if a comprehensive comparison is desired. A simple approach might be to arbitrarily choose a couple of lines within the spherical volume. But the complicated distribution of grey and white matter is critical, allowing for predisposed bias. A better more global approach is obtained by imagining the placement of a test sphere within a cube and then discretizing the cube into 3528 cubic cells, i.e., by breaking each side into 30 increments. After throwing out all the points that fall outside the sphere, 3528 cells remain. The E field is computed at

the centroid of those cells. Because of symmetry, the field is plotted only in one quarter of the volume. The plot begins in the first quadrant, and then switches to the second quadrant at point 1655. The steps correspond to different z positions. The larger step cluster of points are each associated with a new setting for z, while the smaller step clusters constitute a new setting for y as suggested in Fig. 5. The numbered arrows correspond to the order of the planes of points so plotted.

3.3. Inhomogeneous model 2—concentric wedges

Shown in Fig. 6 is yet another model employing a series of spherical wedges. The E field is computed for this model, and compared to that of the homogeneous model in Fig. 7. The mean absolute value of the difference between the two

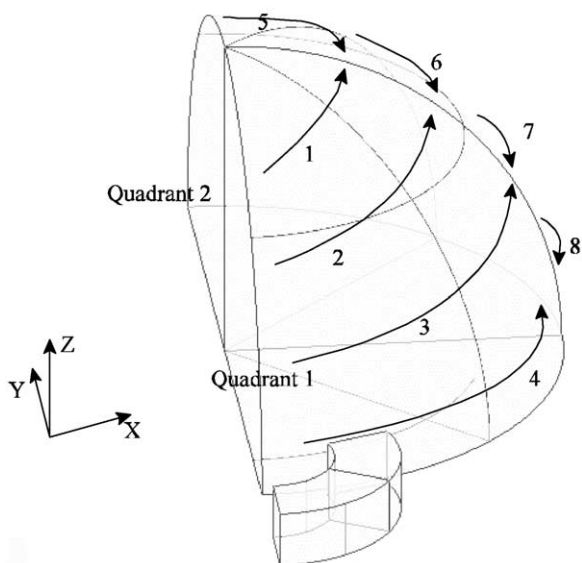


Fig. 5. Order of field point comparison within the volume.

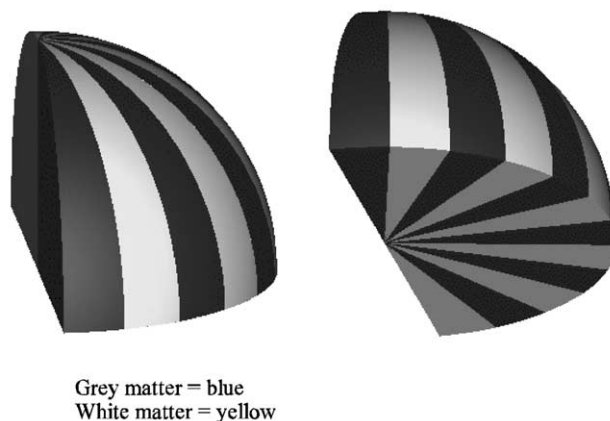


Fig. 6. Brain modeled as a series of spherical wedges, alternating white and grey matter.

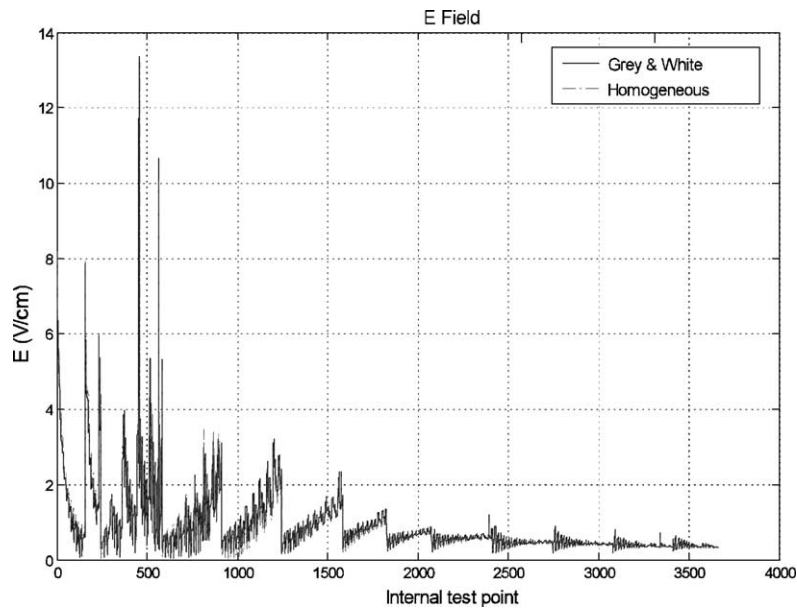


Fig. 7. E field comparison between the wedge shaped model and a homogeneous sphere.

E fields is 7.14%, considering a distribution of 3660 points within the volume.

3.4. Inhomogeneous model 3—concentric wedges with CSF

A final test might suffice to underscore the point being made that paying attention to the distribution of mater in the brain is unwarranted. Baumann et al. (1997) have shown that the electrical conductivity of cerebral spinal fluid is 1.45 S/m at room temperature (25 °C) and 1.79 S/m at body temperature (37 °C) across the frequency range 10–10 kHz. Using the latter value, consider analyzing another wedge shaped model of the brain, this time with CSF distributed in equal volume with white and grey matter as suggested in Fig. 8. In this extreme case, the volume of CSF is assumed to be equal to that of grey and white matter. The difference between the E fields, shown in Fig. 9, increases to a mean absolute value difference of 15.2% due to the higher conductivity of the cerebral spinal fluid. The mean of the difference is only 2.6%. The fact that such an extreme distribution of the three returns such a small difference supports the claim that efforts to accurately model the brain's composition is unwarranted.

3.5. Bounding the maximum electric field variations

When the region of dissimilar conductivity fits totally within another medium, the E field departure from the homogeneous case will be greatest at the point where no tangential electric field exists. The E field will always decrease on the side of the boundary with the smaller conductivity and increase by an equal amount on the side of

the larger conductivity, insuring that the normal current density be continuous. For the case of white and grey matter, the maximum departure from the homogeneous case is $0.7/0.48 = 1.458$. So the maximum E field departure will be -22.9% from the homogeneous case on one side and $+22.9\%$ on the opposite side. If a finger like projection of grey matter exists within white matter with a dominant \times directed electric field, as suggested in Fig. 10, the change in electric field will be greatest at the ends of the projection. At those points where the induced electric field is tangential to the interface, no change from the homogeneous case will be witnessed.

4. Conclusions

As long as the tissue conductivity differences are small, two homogeneous models will deliver the same induced E

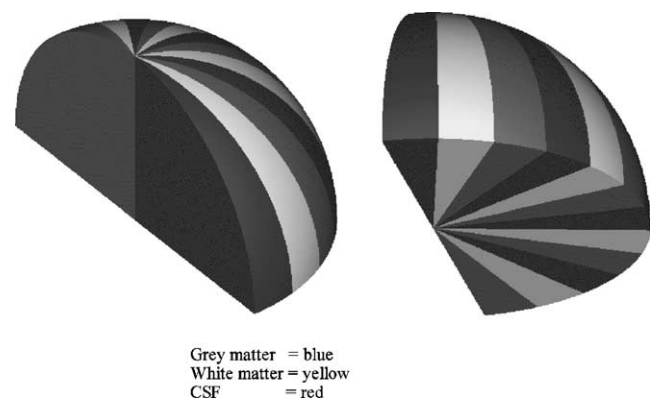


Fig. 8. Combination of white, grey and cerebral spinal fluid.

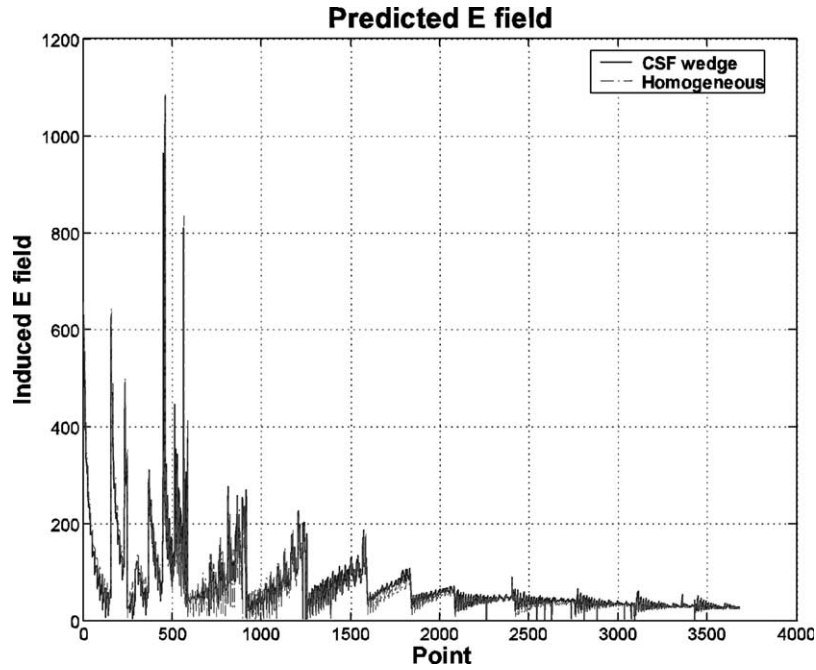


Fig. 9. Induced E field predicted with the wedge model interspliced with CSF.

field regardless of the conductivity distribution. The word small applies when the magnetic field generated by the currents induced is insignificant compared to the stimulation field. The total integrated E field around a loop is fixed by

the primary B field. Two models were analyzed containing well defined borders between white and grey matter. Rather extreme distributions of matter in the brain were assumed to determine that the induced fields have a mean variance from

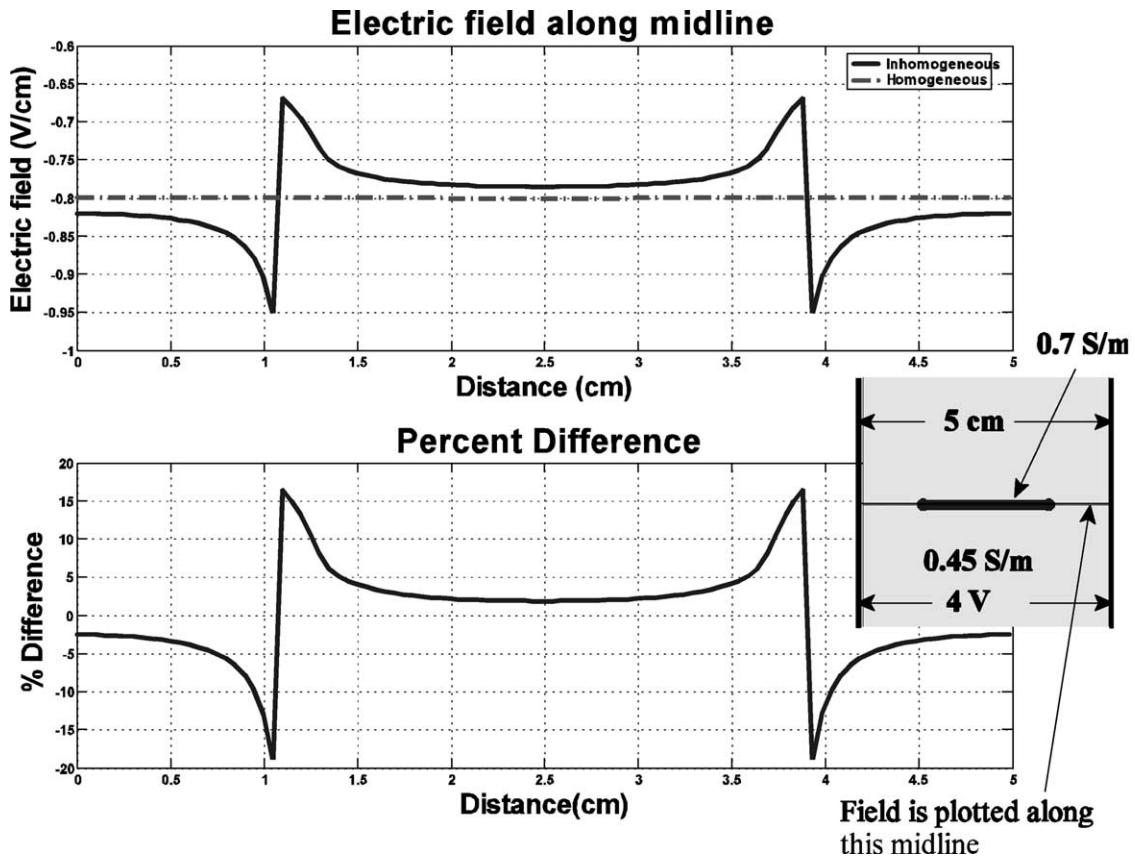


Fig. 10. Electric field change along the midline of a finger like projection of grey matter within white matter.

the homogeneous field of about 7% for white and grey matter, and 15% when cerebral spinal fluid is added. The boundary condition that the normal current density must be continuous dictates the maximum departure from the homogeneous electric field case of 1/2 the ratio of the conductivities of the media involved.

Limitations of these models need to be understood in order to properly interpret these findings. Grey matter has an anisotropic conductivity. Although the calculations were performed using isotropic approximations, the invariance of the induced E field suggests that such differences would not affect the conclusions. The complex patterns of human brain involving gyral folding and layering were not modeled. Additionally, other factors will contribute to whether nerve cells are affected by TMS, including myelination and fiber orientation and morphometry relative to the TMS field (Amassian et al., 1992; Levy et al., 1991).

Acknowledgements

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